# P204: Zero-Shot Self-Supervised Joint Temporal Image and Sensitivity Map Reconstruction via Linear Latent Space

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# Abstract

Introduction

 T2-shuffling is widely used to resolve temporal signal dynamics in FSE acquisitions via linear latent space and a predefined regularizer.

Recent self-supervised learning methods in an unrolled manner achieve high-fidelity reconstructions by learning a regularizer from the undersampled data without a standard supervised training data set.

# Methodology

**Self-supervised reconstruction for single image** 



 $\mathbf{Z}^{(i-1)} = \mathcal{D}_{\mathbf{I}}\left(\mathbf{X}^{(i-1)}\right)$ 

# **Results for realistic FSE MRI:** R = 16, 12 coils, T=32 echoes, echo spacing of 11.5ms

Results





 In this work, we propose a novel approach that utilizes a self supervised learning framework to learn a regularizer constrained on a linear latent space which improves timeresolved FSE images reconstruction quality. Additionally, in regimes without groundtruth sensitivity maps, we propose joint estimation of coil-sensitivity maps using an iterative reconstruction technique.

We perform experiments on simulated and retrospective invivo data to evaluate the performance of the proposed zeroshot learning method for temporal FSE reconstruction.

 $\mathbf{X}^{(i)} = rg\min_{\mathbf{X}} \left\| \mathbf{Y}_{\mathbf{\Theta}} - \mathbf{M}_{\mathbf{\Theta}} \mathbf{FSX} 
ight\|_{2}^{2} + \mu \left\| \mathbf{X} - \mathbf{Z}^{(i-1)} 
ight\|_{2}^{2}$  $= \left( \left( \mathbf{M}_{\boldsymbol{\Theta}} \mathbf{F} \mathbf{S} \right)^{H} \left( \mathbf{M}_{\boldsymbol{\Theta}} \mathbf{F} \mathbf{S} \right) + \mu \mathbf{I} \right)^{-1} \left( \left( \mathbf{M}_{\boldsymbol{\Theta}} \mathbf{F} \mathbf{S} \right)^{H} \mathbf{Y}_{\boldsymbol{\Theta}} + \mu \mathbf{Z}^{(i-1)} \right)$ **Self-supervised reconstruction for FSE with linear** subspace  $\mathbf{Z}_{\mathbf{I}}^{(i-1)} = \mathcal{D}_{\mathbf{I}}\left(oldsymbol{lpha}^{(i-1)}
ight)$  $\mathbf{Z}^{(i-1)} = \mathcal{D}_{\mathbf{I}}\left(\mathbf{X}^{(i-1)}\right)$  $\mathbf{X}^{(i)} = \arg\min_{\mathbf{X}} \|\mathbf{Y}_{\mathbf{\Theta}} - \mathbf{M}_{\mathbf{\Theta}} \mathbf{FSX}\|_{2}^{2} + \mu \left\|\mathbf{X} - \mathbf{Z}^{(i-1)}\right\|_{2}^{2} \ \boldsymbol{\alpha}^{(i)} = \arg\min_{\mathbf{X}} \|\mathbf{Y}_{T\mathbf{\Theta}} - \mathbf{M}_{\mathbf{\Theta}} \mathbf{FS\Phi} \boldsymbol{\alpha}\|_{2}^{2} + \mu_{I} \left\|\boldsymbol{\alpha} - \mathbf{Z}_{\mathbf{I}}^{(i-1)}\right\|_{2}^{2}$ Linear Latent Space defined by SVD Self-supervised reconstruction for FSE for sensitivity maps estimation

 $\mathbf{Z}_{\mathbf{C}}^{(i-1)} = \mathcal{D}_{\mathbf{C}}\left(\mathbf{S}^{(i-1)}\right)$ 

$$\mathbf{S}^{(i)} = \arg\min_{\mathbf{S}} \|\mathbf{Y}_{T\Theta} - \mathbf{M}_{\Theta} \mathbf{F} \mathbf{X}_{\mathbf{T}} \mathbf{S}\|_{2}^{2} + \mu_{C} \left\|\mathbf{S} - \mathbf{Z}_{\mathbf{C}}^{(i-1)}\right\|_{2}^{2} + \lambda_{C} \left\|\mathbf{D} \mathbf{S}\right\|_{2}^{2}$$

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T2-shuffling has demonstrated success in resolving temporal images from volumetric FSE acquisitions which exploits correlations with a low-dimensional subspace temporal **model**, and utilizes a predefined regularizer.



To train models without ground truth, Yaman et al. proposed a self-supervised learning reconstruction method (SSDU), which trains models in a self-supervised fashion by partitioning under-sampled kspace data into two disjoint sets,  $\Theta$  and  $\Lambda$ , and training a network as a regularizer in the traditional optimizations with the information from  $\Theta$  to predict the unseen data,  $\Lambda$ .

#### x and S are commutable

## **Pipeline for joint reconstructions of FSE images** and sensitivity maps



### Results

### **Results for simulated FSE MRI:** R = 24, 8 coils, T=80 echoes, echo spacing of 5.56ms

with groundtruth S-maps without groundtruth S-maps Shuffling SSDU Ours-sub Shuffling Ours-sub Ours-joint GT





• In this work we proposed a novel zero-shot self-supervised reconstruction framework on a linear latent space to simultaneously learn a regularizer from the highly undersampled data itself and exploit temporal correlations to significantly reduce degrees of freedom in the reconstruction.

Moreover, a self-supervised sensitivity estimation stage is proposed which only utilizes the acquired data to further shorten the total scanning time.

Acknowledgements

Conclusion

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